

The Ludic Fallacy

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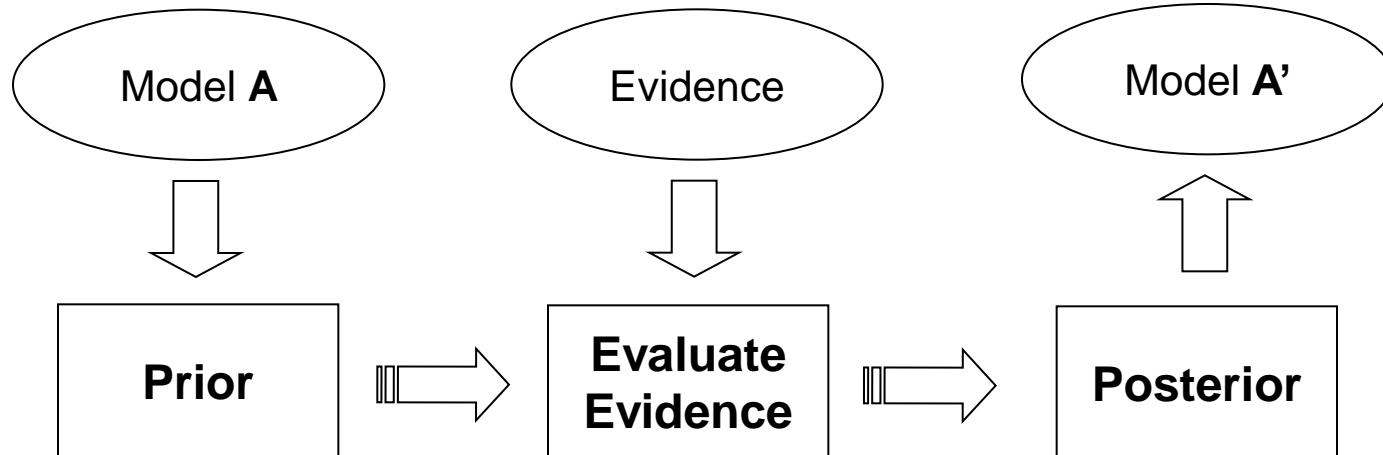
“The attributes of uncertainty we face in real life have little connection to the sterilized ones we encounter in exams and games.”

— Nassim Taleb

Summary

Real problems are not just games of chance

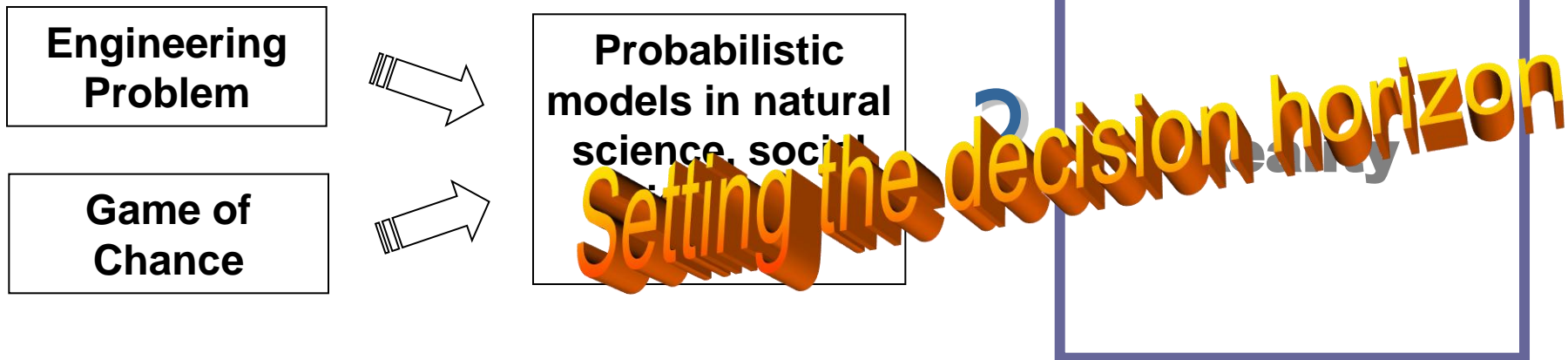
- Re-frame probability and rationality
- “TaleBayesianism”



- Probabilities
- Parameters
- **The Model itself**

The Ludic Fallacy

- Nassim Taleb argues that problems in real life are not necessarily represented as games of chance
 - We don't know the space of possibilities
 - We can't calculate the numbers



“The game of roulette is not subject ... to uncertainty. The sense in which I am using the term [uncertain] is that in which ... there is no scientific basis on which to form a calculable probability whatever.”

— J M Keynes

Problem known but forgotten!

“Decision is a choice amongst the delimited and prescribed moves in a game with fixed rules and a known list of outcomes of any move or sequence of moves.”

— G L S Shackle

Does it matter?

Yes, because otherwise:

- We think we understand the world better than we really do
- We use inappropriate models
- This exposes us to future unknown risk

Structure

- Probability
- Uncertainty
- Rationality
- Omniscience?
- Taleb's demon

Probability

What is Probability?

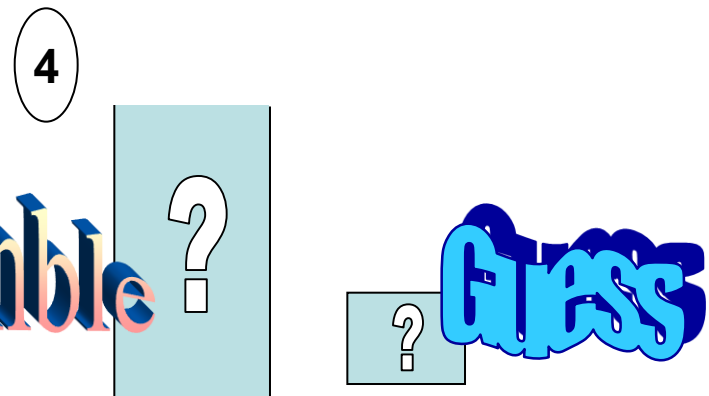
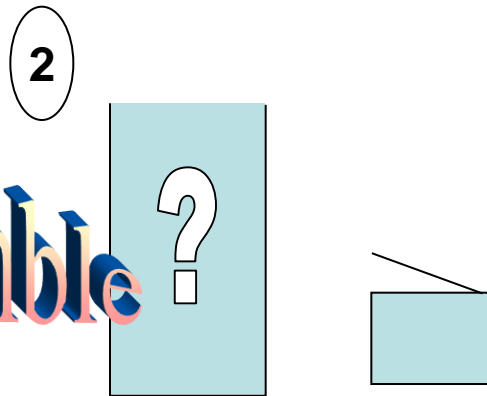
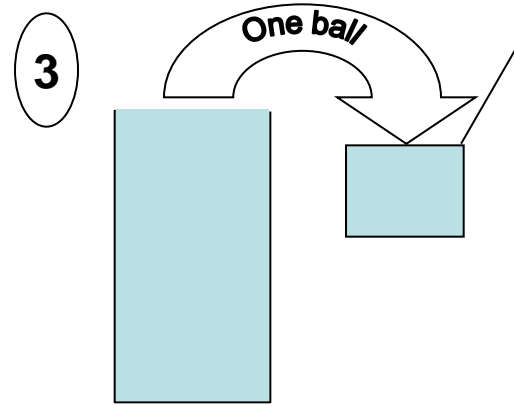
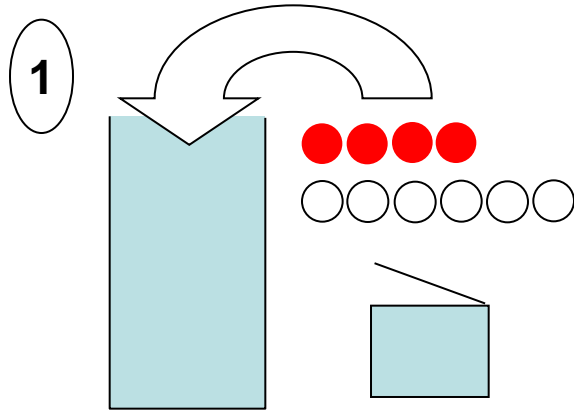
- The definition I will use is that probability consists of:
 - A set of individual possibilities (outcomes or events or worlds)
 - Individuals and combinations form a “space” of possibilities
 - A measure on this space to the interval $[0,1]$
- This is Kolmogorov’s starting point

Interpretations of Probability

- Frequentist
 - Hypothetical ensemble of outcomes of a repeatable experiment
 - The probability measure represents relative frequency
- Subjective
 - Space of possible worlds
 - The probability measure represents “subjective” degree of belief
 - “Subjective” has to be rational in a defined sense of decisions and utility (e.g. Savage axioms)
 - These include the “Sure Thing Principle”

Uncertainty

Aleatory and Epistemic Uncertainty



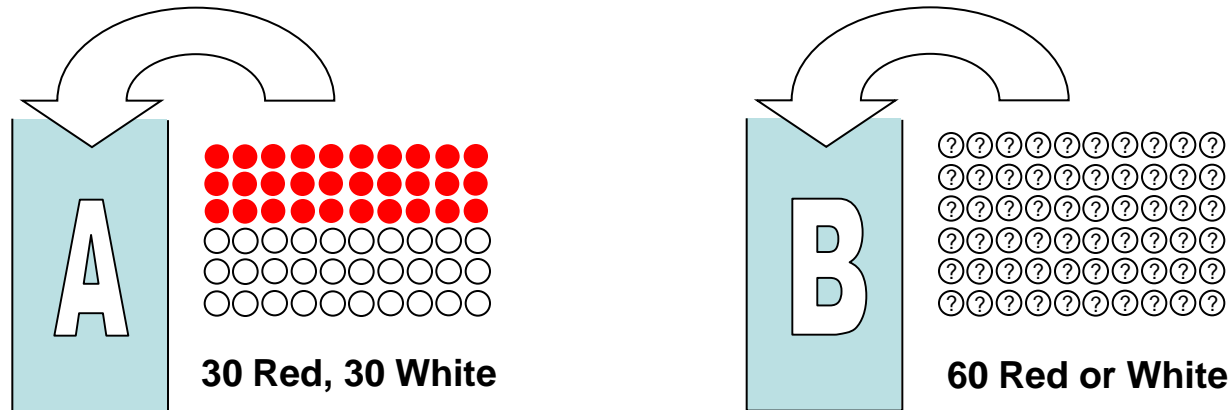
White 60%
Red 40%

60% 60%
40% 40%

Aleatory and Epistemic Uncertainty

- Aleatory Uncertainty
 - Like a game of chance (2) – we can make a choice from a space of possibilities
- Epistemic Uncertainty
 - From lack of knowledge (4) – there is only one ball, we just don't know which one
 - In the absence of any other information assume equally likely (equiprobabilities)
- Yet we do not view these two types of uncertainty with the same confidence ...

Ellsberg Paradox



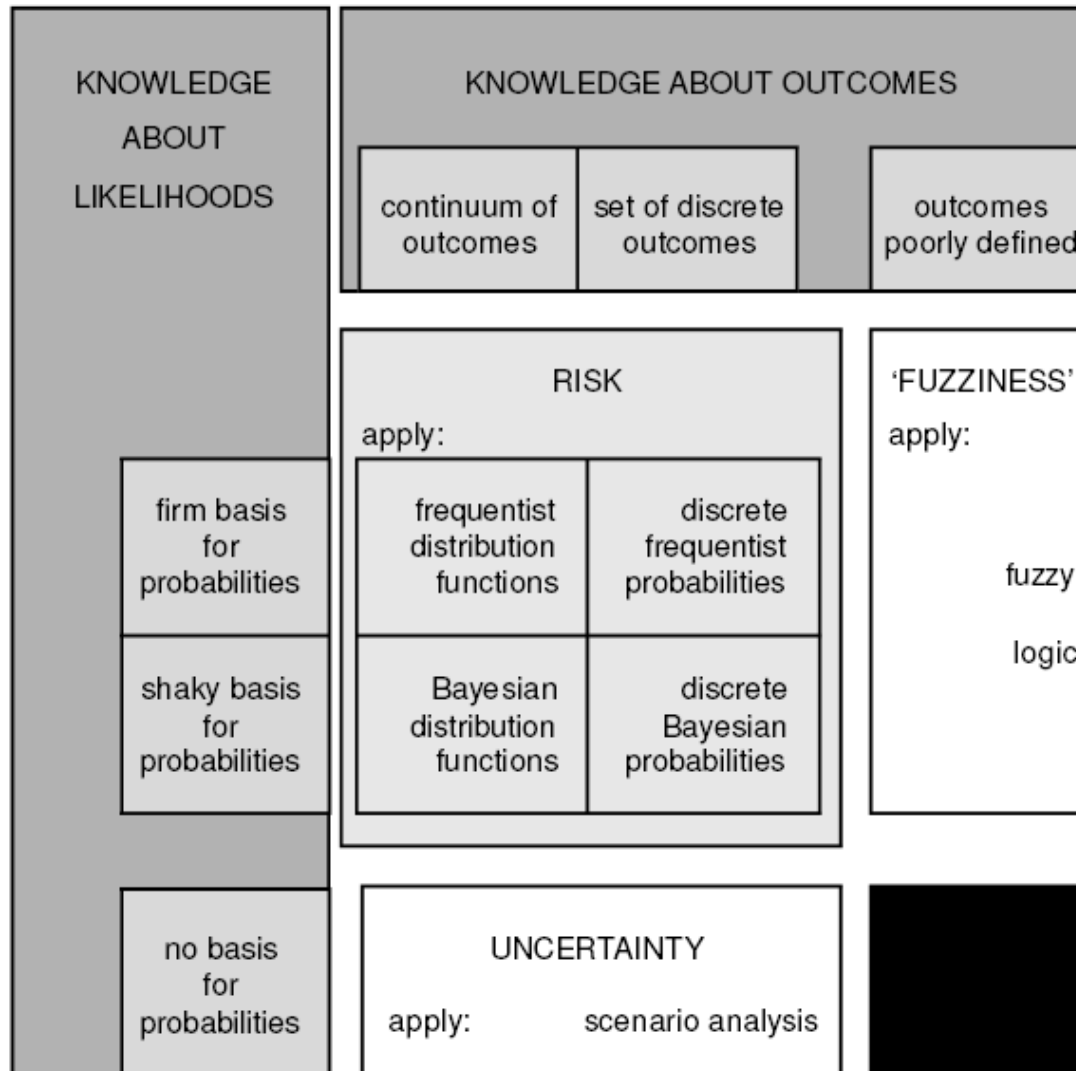
You win £100 if you pick a white ball				You win £100 if you pick a red ball			
Urn A		Urn B		Urn A		Urn B	
Winnings	Choice	Winnings	Choice	Winnings	Choice	Winnings	Choice
£100	50%	£100	?%	-	50%	-	?%
-	50%	£100	100-?%	£100	50%	£100	100-?%

People mostly choose the Urn with the **aleatory** not **epistemic** risk
 Even switching colour, still choose aleatory Urn !

The Jargon of Uncertainty

Intrinsic to system (e.g. prior to an event)	Aleatory / Type A / Stochastic / Natural Variability / Irreducible
Knowledge of system (e.g. after an event)	Epistemic / Type B / Subjective / Reducible
Within Model of system	Parameter
Across Models of system	Model

Risk, Uncertainty, and Ignorance



Rationality

Sure Thing Principle

A. 2 tickets to football;
£100 if it rains

or

B. 2 tickets to rugby;
£100 if it rains

A. 2 tickets to football;
£0 if it rains

or

B. 2 tickets to rugby;
£0 if it rains

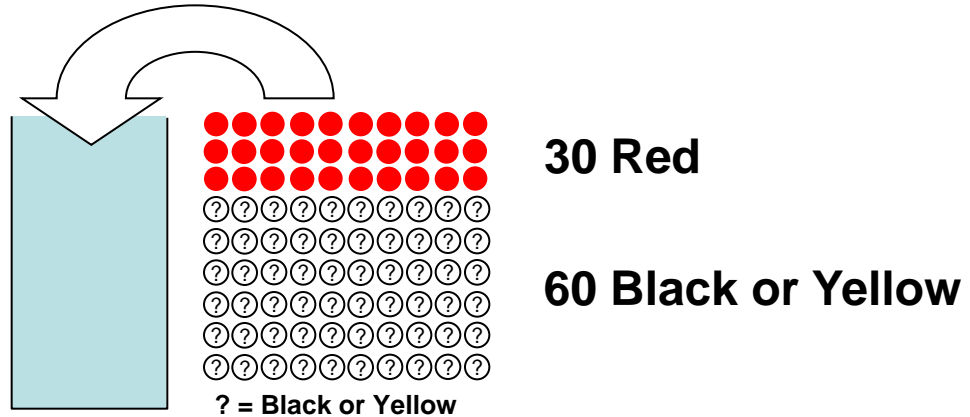
Do you make the same decision?

**If so, the decision is a “sure thing”
independent of events that offer the same payoff
(in this case the payment if it rain)**

Invariance

- What if the Sure Thing Principle WAS valid?
 - Elements of the outcomes that are identical (e.g. the payment in case of the rain) would not affect the decision or gamble or probability
- What if it WASN'T valid?
 - It would mean that decisions (or gambles or probabilities) would depend on common circumstances or consequence
- The latter does sound vaguely plausible for real life

Ellsberg Paradox Ila

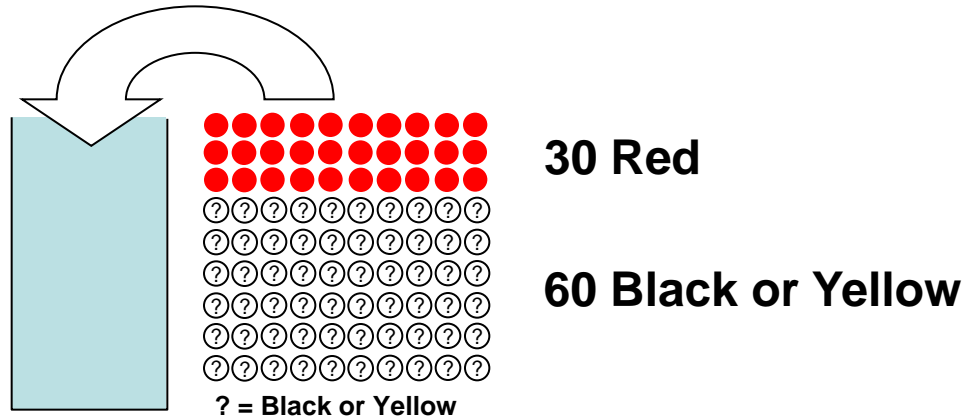


Experiment 1				Experiment 2			
Gamble A		Gamble B		Gamble C		Gamble D	
Winnings	Choice	Winnings	Choice	Winnings	Choice	Winnings	Choice
£200	Red	£200	Black	£100	Red or Yellow	£100	Black or Yellow

Red is an **aleatory** gamble
 Black is an **epistemic** gamble

Black or Yellow is an **aleatory** gamble
 Red or Yellow is an **epistemic** gamble

Ellsberg Paradox - IIb



Experiment 1				Experiment 2			
Gamble A		Gamble B		Gamble C		Gamble D	
Winnings	Choice	Winnings	Choice	Winnings	Choice	Winnings	Choice
£200	Red	£200	Black	£100	Red or Yellow	£100	Black or Yellow

The second Experiment differs only in that it includes Yellow.
 People prefer the “sure thing” which confounds the “Sure Thing Principle”!

Allais Problem

Experiment 1				Experiment 2			
Gamble A		Gamble B		Gamble C		Gamble D	
Winnings	Chance	Winnings	Chance	Winnings	Chance	Winnings	Chance
\$500	1%	\$0	1%	\$500	1%	\$0	1%
\$500	10%	\$2,500	10%	\$500	10%	\$2,500	10%
\$500	89%	\$500	89%	\$0	89%	\$0	89%

er, how did that work again?

Experiment 1				Experiment 2			
Gamble A		Gamble B		Gamble C		Gamble D	
Winnings	Chance	Winnings	Chance	Winnings	Chance	Winnings	Chance
\$1m	100%	\$5m	10%	\$1m	11%	\$5m	10%
		\$1m	89%				
\$1m		\$1.39m		\$110k		\$500k	

and remind me of the point ...

Experiment 1				Experiment 2			
Gamble A		Gamble B		Gamble C		Gamble D	
Winnings	Chance	Winnings	Chance	Winnings	Chance	Winnings	Chance
\$500	1%	\$0	1%	\$500	1%	\$0	1%
\$500	10%	\$2,500	10%	\$500	10%	\$2,500	10%
\$500	89%	\$500	89%	\$0	89%	\$0	89%

Rationality

- Are our decisions therefore irrational?
- Or do we suspect the formal model may not be a complete description of reality?
- Would it be rational to expect:
 - The context to affect decisions?
 - To play safe when there are (unstated) chances outside our expectation of (downside) risk?

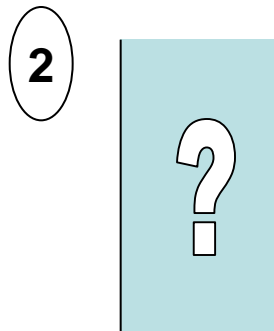
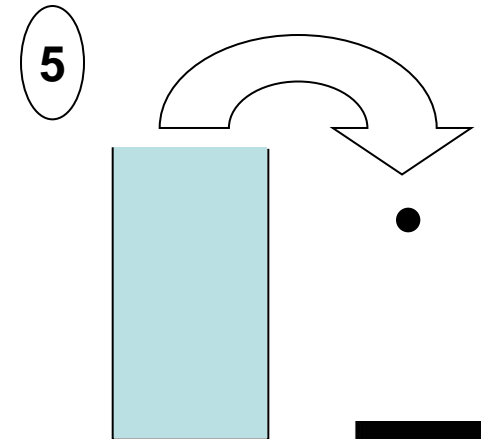
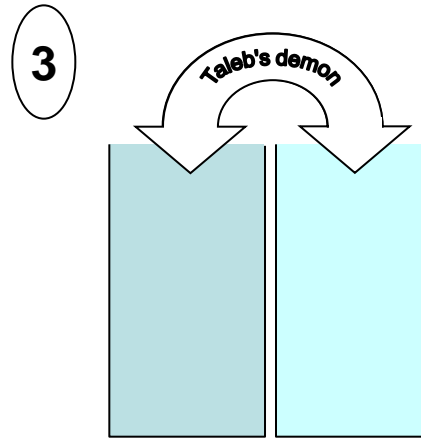
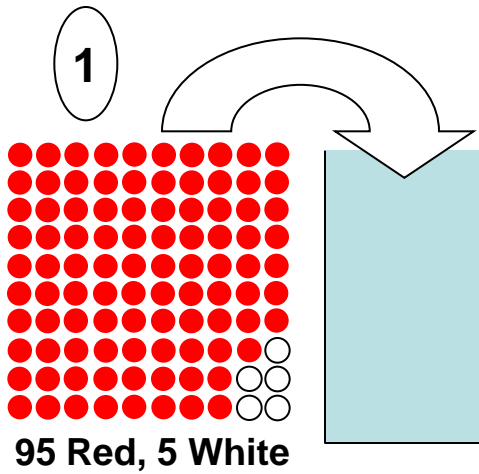
Omniscience?

Omniscience?

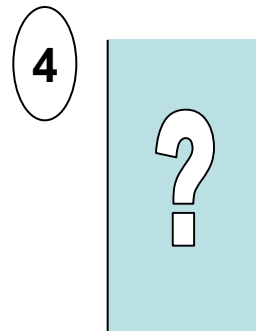
- Can we know everything?
 - In practice?
 - In principle?
- Argument
 - Suppose we could know the space of possibilities, then we can't know if there is another
- If we can't
 - We can't know the space of possibilities

Taleb's Demon

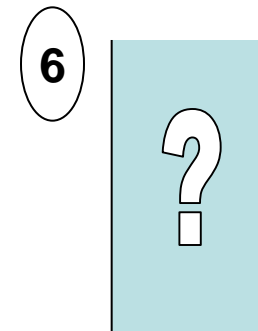
Talebian Uncertainty



White 5%
Red 95%



Odds of a
white?



Odds of a
black?



Taleb's demon

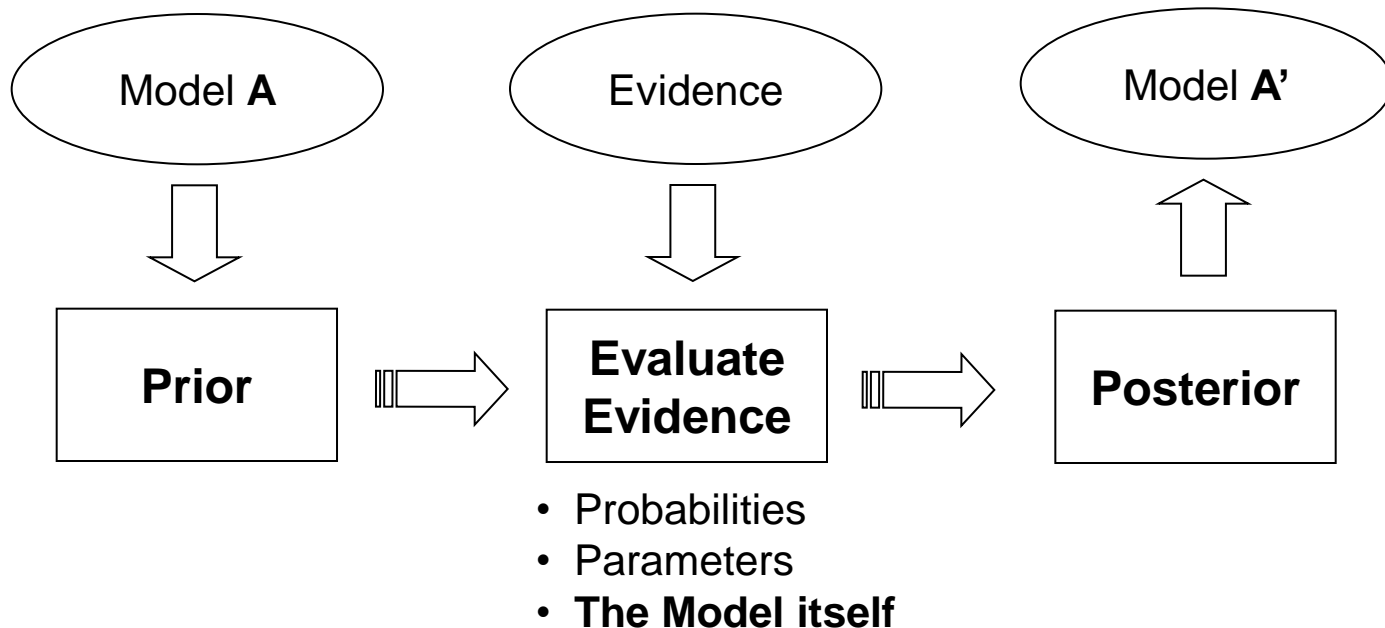
- Initially we have Aleatory Uncertainty
 - Usual probability theory applicable (2)
- A demon can change the balls
 - We no longer know the space of possibilities (3 & 4)
 - But the principle of equiprobabilities would leave the odds the same if there were no new balls introduced or balls taken away
- Then we discover a black ball
 - We know something we didn't know but not what has happened to the space of possibilities (5 & 6)

If you believe in Taleb's demon

- Epistemic uncertainty need not have the same sample space as aleatory uncertainty
 - so if you believe that epistemic uncertainty is uncomfortable you'll vote for the aleatory option
- The Sure Thing Principle need not hold
 - Taleb's demon could change the context - the space of probabilities
 - If you suspected this, your decision would depend on the context
- You would then be a "TaleBayesian"
 - Prepared to reconsider the space of possibilities **and the model** in the light of the evidence

TaleBayesian

Re-consider the model as well as the probabilities or parameters



Conclusion

- Probability models can be incomplete models of reality due to “unknown” changes in the space of possibilities
- This may provide an explanation of apparent irrationality in decision theory
- Be prepared to adopt a context-sensitive approach to uncertainty (TaleBayesian)
- Just a bit of research needed now ...